

# *Present and Future Computing Requirements for Ab Initio Calculations of Nuclear Reactions and Light Exotic Nuclei*

*Large Scale Computing and Storage Requirements for Nuclear Physics (NP): Target 2017*

*April 29-30, 2014*

S. Quaglioni

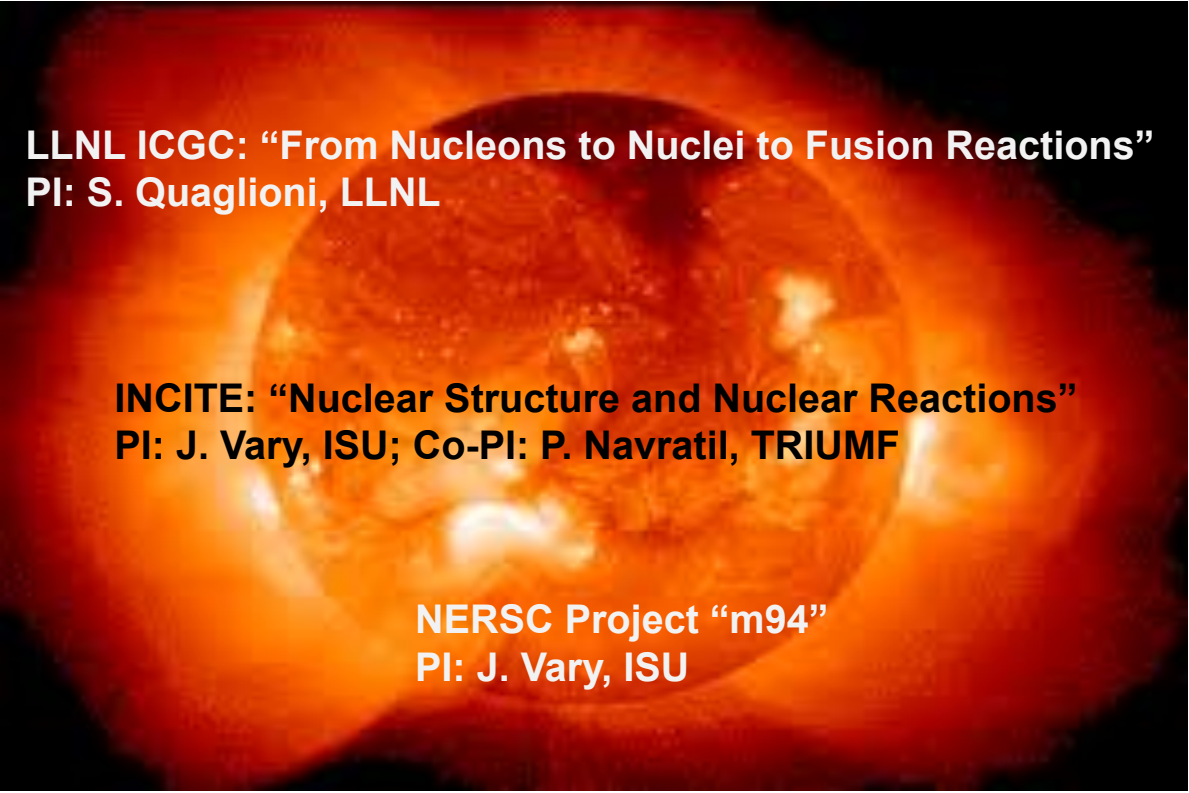


## **Contributors:**

G. Hupin (LLNL)  
P. Navratil, C. Romero-Redondo (TRIUMF)  
R. Roth, J. Langhammer (TU Darmstadt)

IM #774417

This work was performed under the auspices of the U.S. Department of Energy by Lawrence Livermore National Laboratory under contract DE-AC52-07NA27344. Lawrence Livermore National Security, LLC

A background image showing a bright, glowing orange and yellow sphere, likely representing a nuclear fusion reaction or a star's core, with a darker, textured surface.

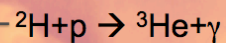
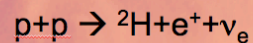
**LLNL ICGC: “From Nucleons to Nuclei to Fusion Reactions”**  
**PI: S. Quaglioni, LLNL**

**INCITE: “Nuclear Structure and Nuclear Reactions”**  
**PI: J. Vary, ISU; Co-PI: P. Navratil, TRIUMF**

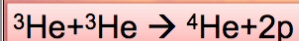
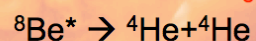
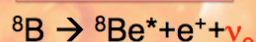
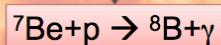
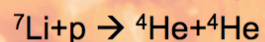
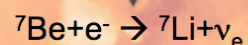
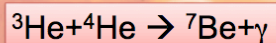
**NERSC Project “m94”**  
**PI: J. Vary, ISU**

# Our goal is to develop a fundamental theory for the description of thermonuclear reactions and exotic nuclei

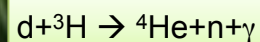
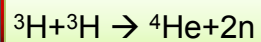
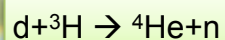
## Standard solar model



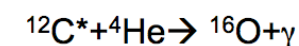
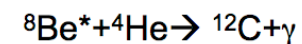
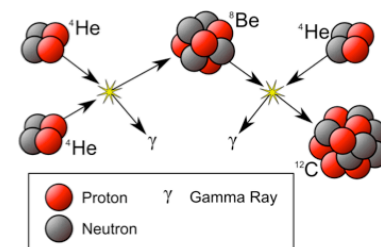
pp chain



## Fusion Energy Generation

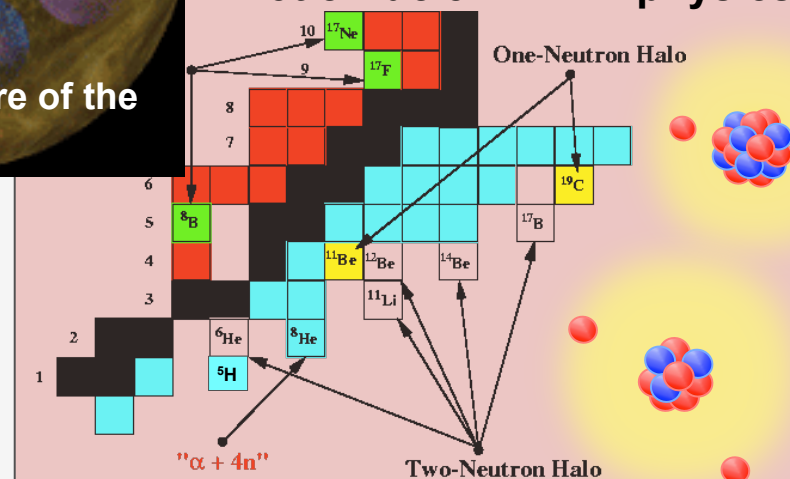


What is the nature of the nuclear force?



## Stellar Nucleosynthesis

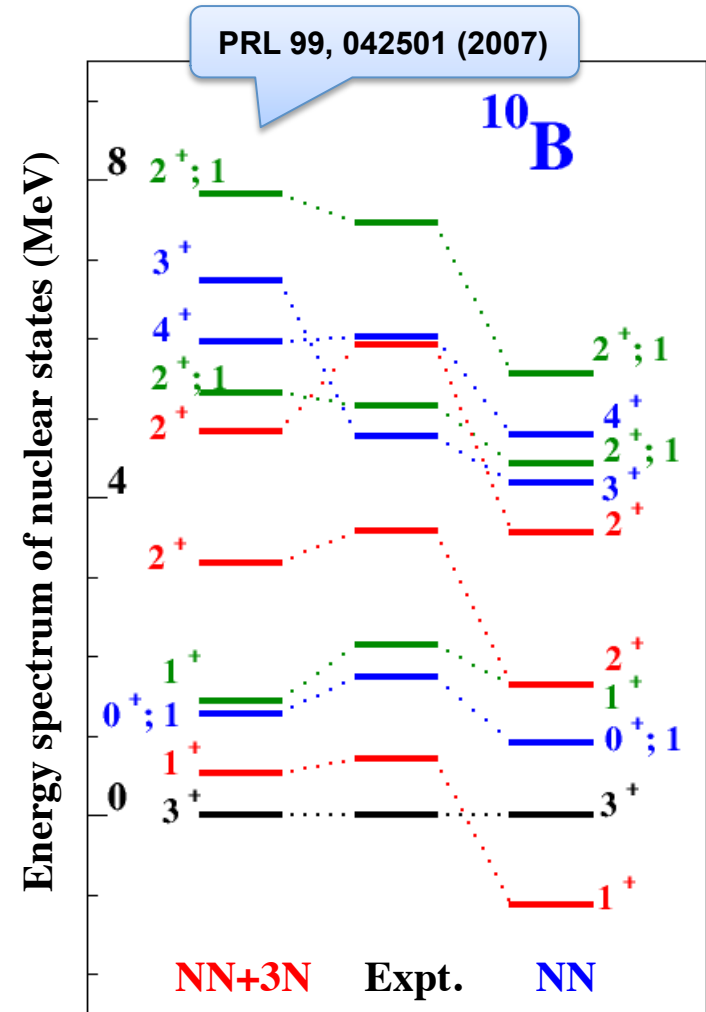
## Exotic Nuclei – FRIB physics



# Large-scale computations have already allowed us to describe static properties of nuclei from first principles

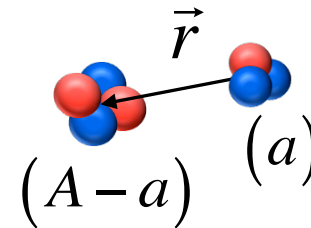
- *Ab initio* no-core shell model (NCSM) approach
  - Bound states
  - Two- and three-nucleon (NN+3N) forces based upon Quantum Chromodynamics

Helped to point out  
the fundamental importance  
of 3N forces in structure  
calculations.



## We extended this approach by adding the dynamics between nuclei with the resonating-group method (RGM)

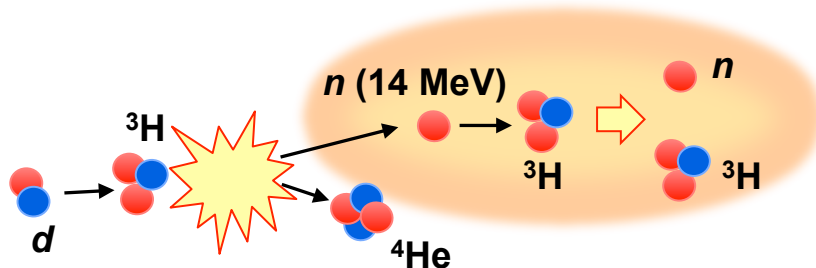
- Reconstruct the interaction potential between a projectile and a target starting from:
  - *Ab initio* NCSM wf. of the clusters
  - Nucleon-nucleon (NN) interactions
- Solve for projectile-target relative motion
- Investments from: DOE/SC/NP, SciDAC-2 (UNEDDEF)



**Pioneered ab initio calculations of light-nuclei fusion reactions starting from NN interactions**

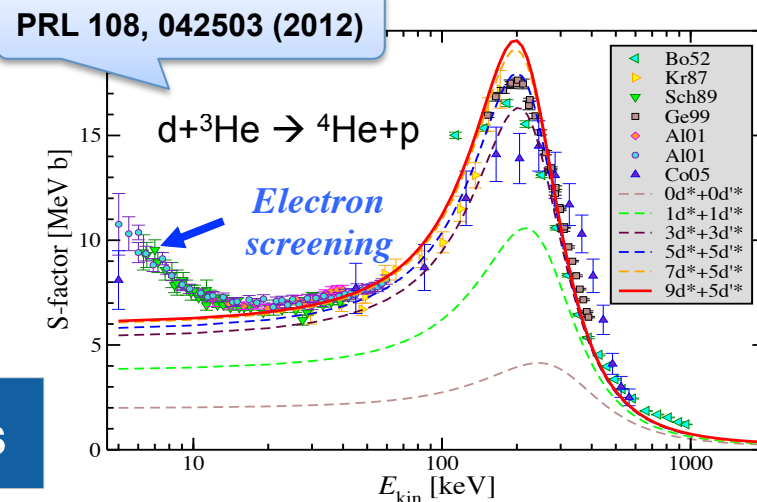
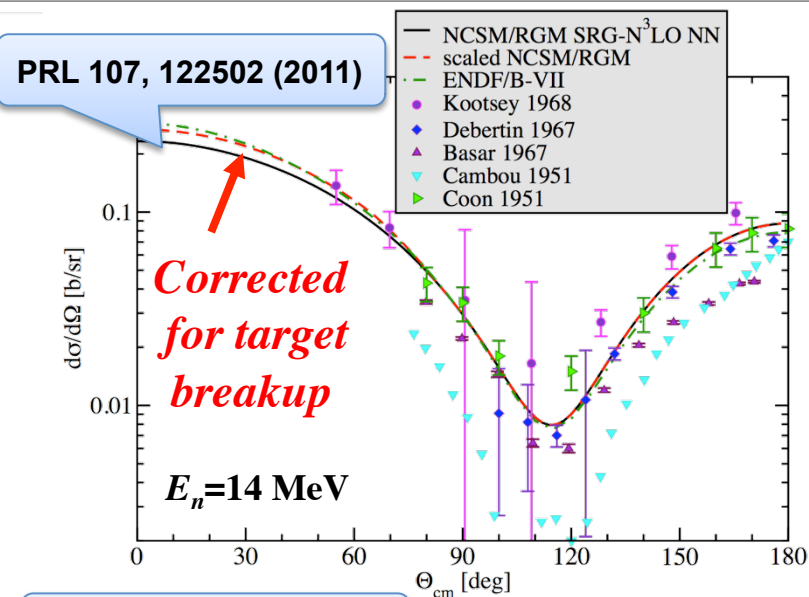
# Started with nucleon-nucleus collisions & gradually built up capability to describe fusion reactions with NN force

- Evaluated  $n+{}^3\text{H} \rightarrow n+{}^3\text{H}$  cross section for fusion diagnostics with required 5% accuracy



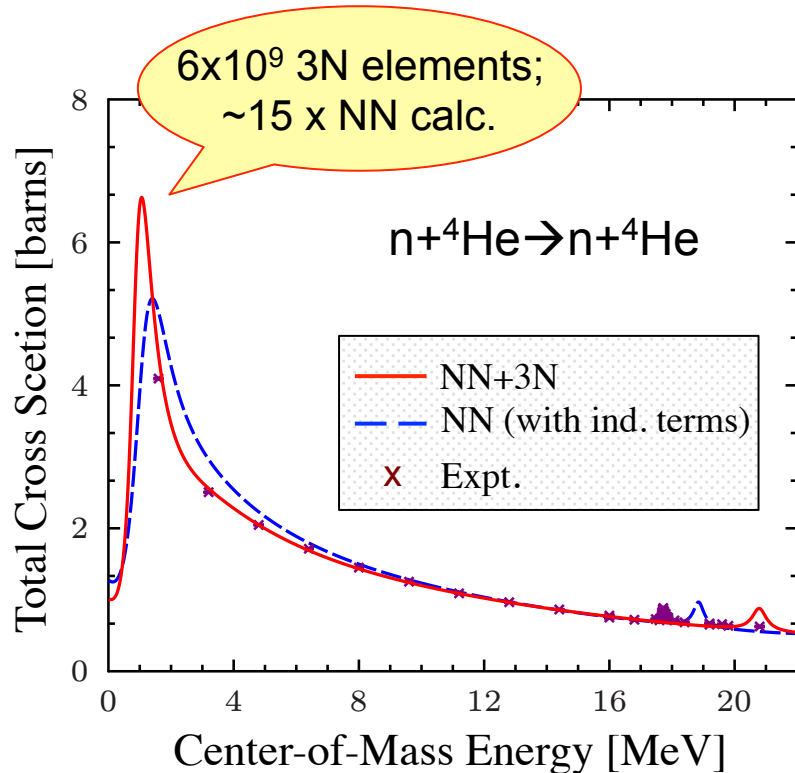
- Deuterium- ${}^3\text{H}$  & deuterium- ${}^3\text{He}$  fusion important for Big Bang nucleosynthesis, fusion research, atomic physics

**To do: 3N force; 3-body dynamics**

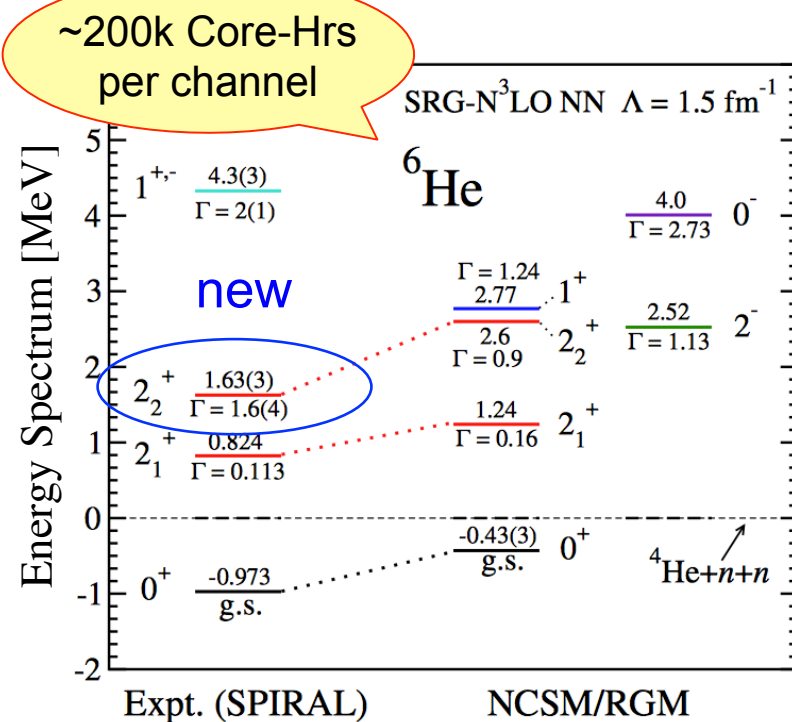
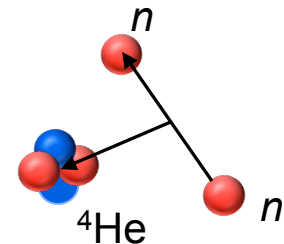


# Now including 3N force in reactions and describing continuum of three clusters (DOE/SC/NP Early Career)

- 3N force needed for high-fidelity simulations



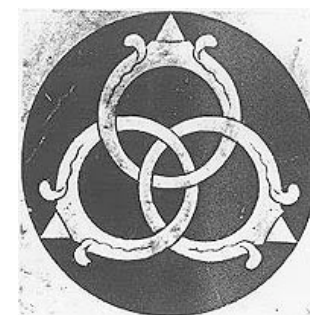
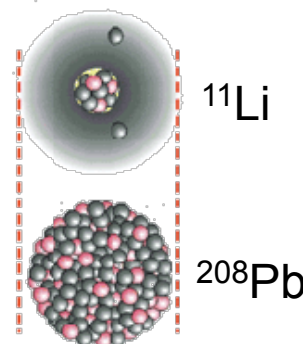
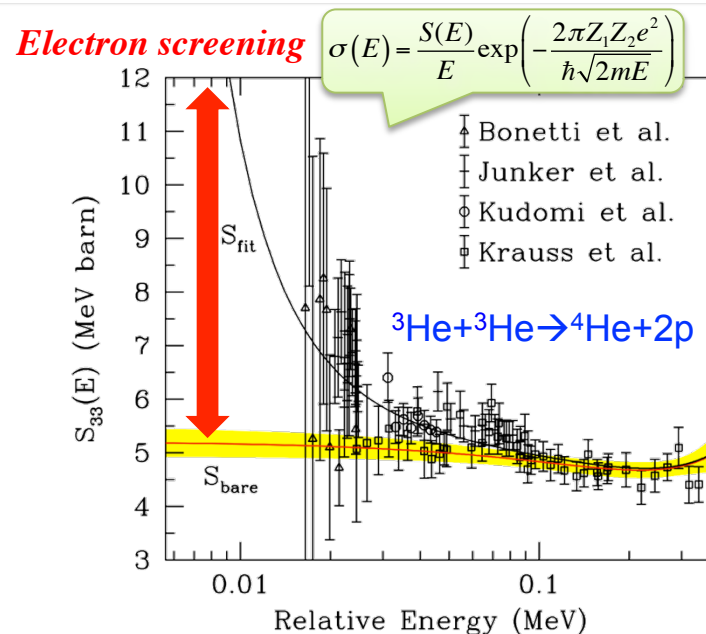
- We want to describe systems with 3-body decay channels





# From now through 2017: deliver high-fidelity simulations complete of both 3N-force & 3-cluster dynamic effects

- **In 2017:**  ${}^3\text{H}+{}^3\text{H}\rightarrow{}^4\text{He}+n+n$  (fusion research) and  ${}^3\text{He}+{}^3\text{He}\rightarrow{}^4\text{He}+p+p$  (solar astrophysics)
  - As an intermediate step calculation with only NN interaction
- **In 2017:** Spectroscopy of Borromean exotic nucleus  ${}^{11}\text{Li}$  as  ${}^9\text{Li}+n+n$  (FRIB physics)
  - At first  ${}^6\text{He}(={}^4\text{He}+n+n)$  and  ${}^5\text{H}(={}^3\text{H}+n+n)$  with NN+3N force



# Our problem, our solution

■ Problem: 
$$\sum_v \int d\vec{r} \left[ H_{v'v}(\vec{r}', \vec{r}) - E N_{v'v}(\vec{r}', \vec{r}) \right] g_v(\vec{r}) = 0$$

Hamiltonian couplings

$$\langle (A-a) | \hat{A}_{v'} H \hat{A}_v | (a) \rangle$$

$$\langle (A-a) | \hat{A}_{v'} \hat{A}_v | (a) \rangle$$

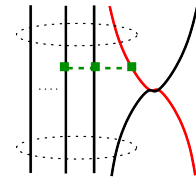
Overlap couplings

- 1) **Input:** NN, 3N interactions; projectile, target wave functions
- 2) **Compute:** Hamiltonian and Overlap couplings
  - Non trivial specialized algebra, depends on projectile mass
  - Sparse matrices; dim = f(# oscillator shells, # projectile nucleons)
  - Sparsity not easily predictable, depends on interaction in input
- 3) **Solve:** 2-, 3-body coupled-channel equations
  - At each energy step: dense linear algebra
- 4) **Output:** Scattering matrix, wave functions, phase shifts



# Our biggest computational challenges come from couplings depending on many-body densities

- Storing in memory many-body density matrices not feasible



**N+(A-1) with 3N interaction**

$$\propto_{SD} \langle \psi_{\alpha_1}^{(A-1)} | a_h^+ a_i^+ a_j^+ a_m a_l a_k | \psi_{\alpha_1}^{(A-1)} \rangle_{SD}$$

## A. Compute and store (coupled) reduced matrix elements

- Efficient when doable
- Only very light systems

$$\sum_{\beta} \langle \psi_{\alpha_1}^{(A-1)} | \left\| (a_h^+ (a_i^+ a_j^+)^{\kappa' \tau'})^{K' T'} \right\| \psi_{\beta}^{(A-4)} \rangle_{SD} \times \langle \psi_{\beta}^{(A-4)} | \left\| ((a_m a_l)^{\kappa \tau} a_k)^{K T} \right\| \psi_{\alpha_1}^{(A-1)} \rangle_{SD}$$

## B. On the fly calculation of (uncoupled) density matrices

- Well suited for parallel computing
- Can address heavier systems

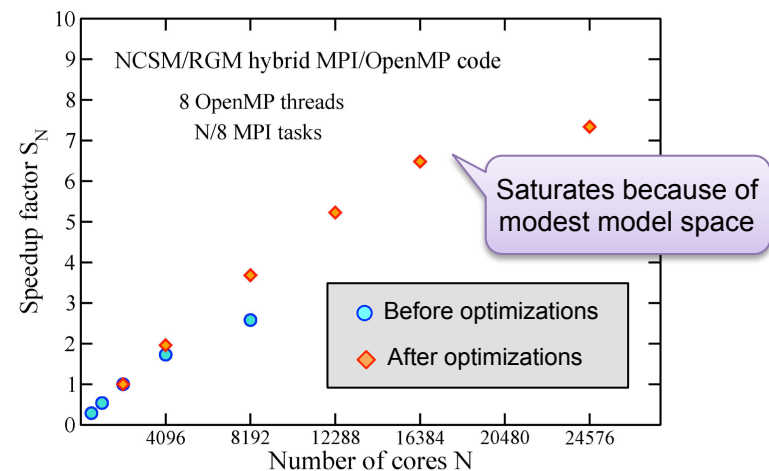
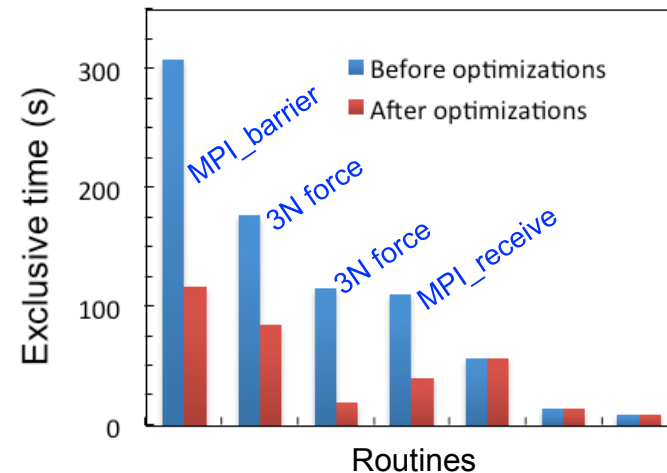
$$| \psi_{\alpha_1}^{(A-1)} \rangle_{SD} = \sum_i | SD \rangle_i$$

**In 2017 we expect to transition more and more towards strategy B.**

# The primary code is NCSM\_RGM, based on strategy A.

- Hybrid MPI/OpenMP
  - up to 98,304 cores on TITAN
- Algorithms include
  - Mostly specialized, in house
  - Matrix multiplications, inversions, diagonalizations
- Recent optimizations include
  - MPI I/O for large input data
  - Hybrid “all slaves” algorithms
  - MKL threaded libraries for dense algebra components

**Excellent scaling should continue in larger model spaces (to study)**



## Current HPC Usage (2012-2013)

- LLNL Institutional Computing Grand Challenge (SIERRA)
  - 1,944 nodes, 12 cores/node
  - 261 teraflop/s, 24 GB/node
- INCITE allocation, PI: J. Vary, co-PI: P. Navratil (TITAN)
  - 10M Core-Hrs, ~70 runs/year
  - Typically 1,000 MPI tasks and 12 OpenMP threads/task for 12 Hrs
- NERSC project “m94”, PI: J. Vary (Edison, early users)
  - 23M Core-Hrs, ~50 runs/year
  - Up to 6,144 nodes for 8 Hrs: 12,288 MPI tasks, 8 OpenMP threads/task (98,304 cores)
- NERSC project “m94”, PI: J. Vary (Edison, early users)
  - 12M Core-Hrs
  - Typically 200-600 nodes, i.e. 3 to 10% of machine
  - Could use 20% now

## Current HPC Usage (2012-2013)

- LLNL Institutional Computing Grand Challenge (SIERRA)
  - 1,944 nodes, 12 cores/node
  - 261 teraflop/s, 24 GB/node
- INCITE allocation, PI: J. Vary, co-PI: P. Navratil (TITAN)
  - Memory Usage:
    - All memory on the node
    - Need at least 2GB/core
    - Use all global memory
  - Data Usage:
    - Input < 100 GB
    - Output < 0.5 TB
    - Use mostly /scrach
- NERSC project “m94”, PI: J. Vary (Edison, early users)

# HPC Requirements for 2017

- Estimate: 15 x (usage for 3-cluster simulations)
  - Selected, more challenging science goals
  - Concurrent storage of 3N matrix elements & 3-cluster configurations
  - Approach under development
  - Unprecedented large scale
  - Store more scattering data for later use
- Minimum 25M Core-Hrs
  - Fewer, larger runs (20-50% of Edison), same typical run time
  - Will need all memory on node, i.e., # MPI tasks = # nodes
    - Use threads with OpenMP
  - Expect algorithmic changes
  - May need more load balancing
  - Larger data requirement

# Summary

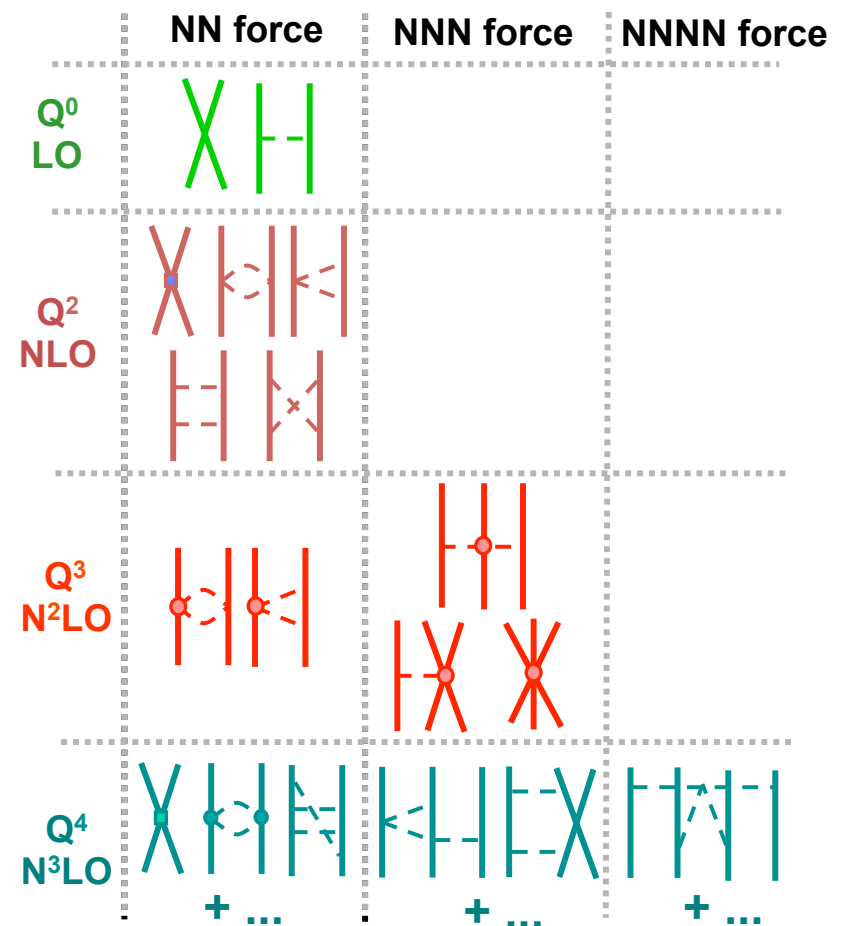
- With HPC we are addressing previously unsolvable problems:
  - ☑ NNN force in light-nucleus reactions
  - ☑ *Ab initio* description of three clusters in the continuum
- **More memory**, larger core count, larger allocations will allow higher-fidelity simulations of complex reactions & exotic nuclei
  - Solar astrophysics, fusion research, FRIB physics
- To achieve these goals and make optimal use of new HPC architectures we will need the help of NERSC experts!
  - Not yet using GPUs (MPI/OpenMP more adapt to our problem);
  - Not porting/optimizing for MIC (Or are we?);
- Need more SciDAC type of support; dedicated positions to foster new generation of computational+nuclear scientists that can help us keep up with new technologies and reach the exascale



# Extras

# Accurate nuclear interactions (and currents)

- Nuclear forces are governed by quantum chromodynamics (QCD)
  - QCD non perturbative at low energies
- Chiral effective field theory ( $\chi$ EFT)
  - retains all symmetries of QCD
  - explicit degrees of freedom:  $\pi$ , N
- Perturbative expansion in positive powers of  $(Q/\Lambda_\chi) \ll 1$  ( $\Lambda_\chi \sim 1$  GeV)
  - nuclear interactions
  - nuclear currents
- Chiral symmetry dictates operator structure
- Low-energy constants (LECs) absorb short-range physics
  - some day all from lattice QCD
  - now constrained by experiment



Worked out by Van Kolck, Keiser, Meissner, Epelbaum, Machleidt, ...

# Major Publications

PRL **110**, 022505 (2013)

PHYSICAL REVIEW LETTERS

week ending  
11 JANUARY 2013

## ***Ab Initio* Description of the Exotic Unbound $^7\text{He}$ Nucleus**

Simone Baroni,<sup>1,2,\*</sup> Petr Navrátil,<sup>2,3,†</sup> and Sofia Quaglioni<sup>3,‡</sup>

PHYSICAL REVIEW C **87**, 034326 (2013)



## **Unified *ab initio* approach to bound and unbound states: No-core shell model with continuum and its application to $^7\text{He}$**

Simone Baroni,<sup>1,2,\*</sup> Petr Navrátil,<sup>2,3,†</sup> and Sofia Quaglioni<sup>3,‡</sup>

PHYSICAL REVIEW C **88**, 034320 (2013)

## **Three-cluster dynamics within an *ab initio* framework**

Sofia Quaglioni,<sup>1,\*</sup> Carolina Romero-Redondo,<sup>2,†</sup> and Petr Navrátil<sup>2,‡</sup>

PHYSICAL REVIEW C **88**, 054622 (2013)

## ***Ab initio* many-body calculations of nucleon- $^4\text{He}$ scattering with three-nucleon forces**

Guillaume Hupin,<sup>1,\*</sup> Joachim Langhammer,<sup>2,†</sup> Petr Navrátil,<sup>3,‡</sup> Sofia Quaglioni,<sup>1,§</sup> Angelo Calci,<sup>2,||</sup> and Robert Roth<sup>2,¶</sup>